

# ROADEF 2010 Challenge

A large scale energy optimization problem

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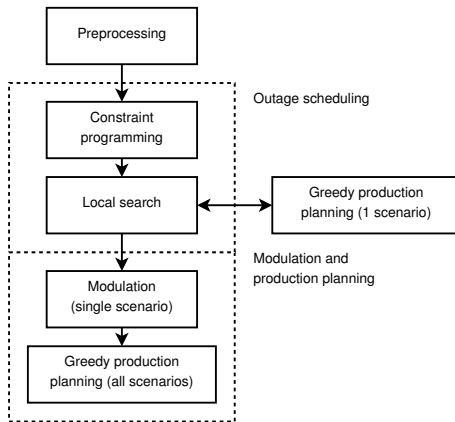
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# Problem introduction

We consider the problem in two parts:

- The outage scheduling part includes:
  - Scheduling constraints (CT13 to CT21) and refueling and fuel level constraints
  - Deciding the number of outages for each type 2 plant
- The production planning part includes:
  - Setting production levels for all scenarios
  - Scenario demand and modulation constraints

# Solution approach



# Constraint programming

The CP-solver (made with the Gecode library) is used to find a feasible starting solution for the outage scheduling part.

- Objective: Maximize average online type 2 capacity
- No demand constraints, no scenarios
- Feasible only with respect to scheduling and fuel constraints
- Output: the number of outages, outage start weeks and refueling amounts

Note: in the qualification round we used the ILOG CP-solver, but for the B-instances we had difficulties finding feasible solutions.

## Constraint programming, cont.

Variables:

- Outage scheduled,  $\{0, 1\}$
- Outage start week,  $\{0, \dots, H - 1\}$
- Refueling amounts,  $\{R_{min}, \dots, R_{max}\}$

Constraints:

- CT13 to CT21
- Minimum spacing constraints to ensure existence of a feasible refueling schedule

# Branching strategy

		Outages			
		0	1	...	K-1
Type 2 plants in random order	0				
	1				
	...				
	I-1				

# Branching strategy, cont'd.

		Outages			
		0	1	...	K-1
Type 2 plants in random order	0				
	1				
	...				
	I-1				



# Branching strategy, cont'd.

		Outages			
		0	1	...	K-1
Type 2 plants in random order	0				
	1				
	...				
	I-1				

# Branching strategy, cont'd.

		Outages			
		0	1	...	K-1
Type 2 plants in random order	0				
	1				
	...				
	I-1				

# Branching strategy, cont'd.

		Outages			
		0	1	...	K-1
Type 2 plants in random order	0				
	1				
	...				
	I-1				

## Branching strategy, cont'd.

		Outages			
		0	1	...	K-1
Type 2 plants in random order	0				
	1				
	...				
	I-1				

## Branching strategy, cont'd.

- ① Outages scheduled: First branch is on *scheduled*
- ② Start week: First branch is on *earliest week*
- ③ Refuel amount: First branch is on *maximal refuel amount*

# Greedy production planning

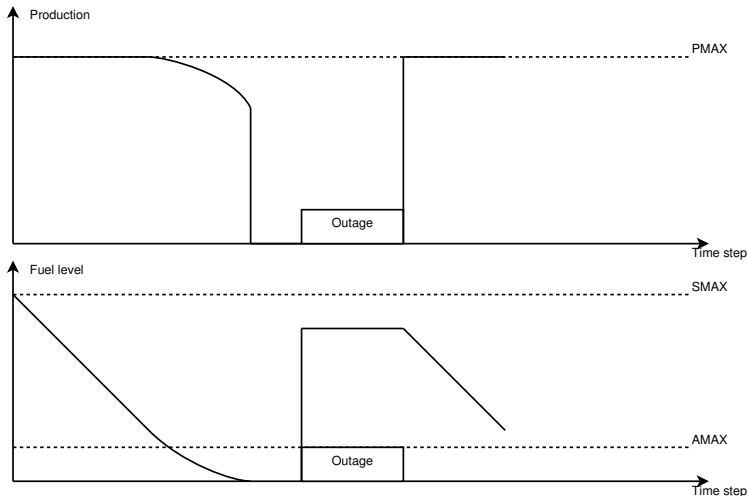
For type 2 plants

- Find feasible production levels
- Increasing refueling amounts

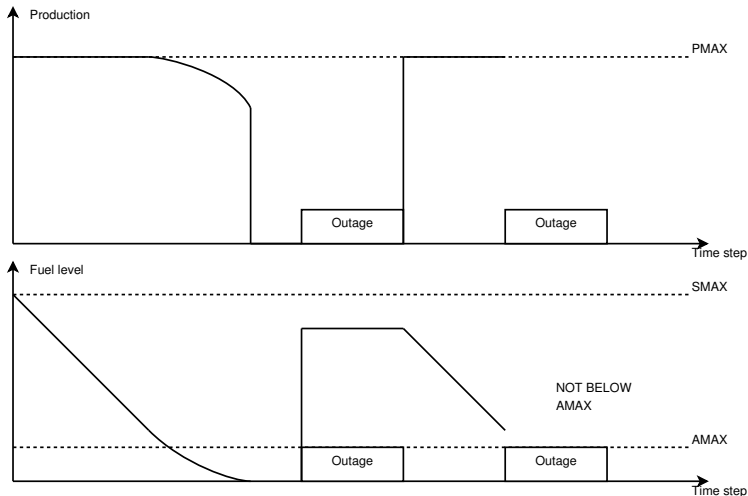
For type 1 plants

- Cheapest type 1 plant is used first
- Production levels are only set after modulation have been performed and just before writing the final solution

## Greedy production planning, cont'd

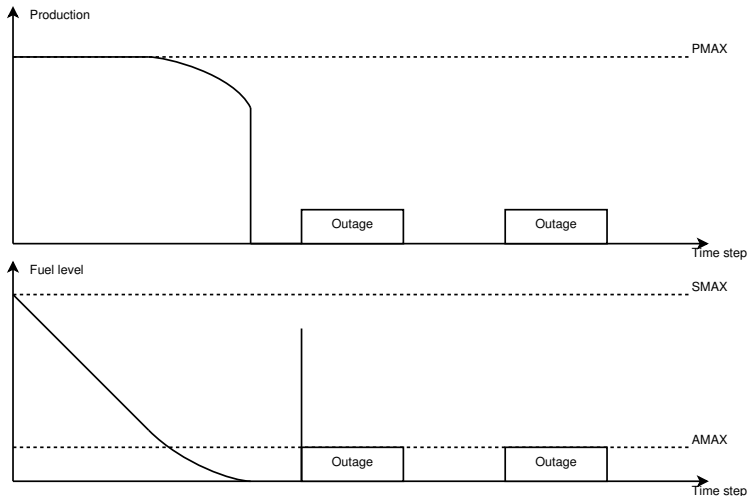


# Greedy production planning, cont'd

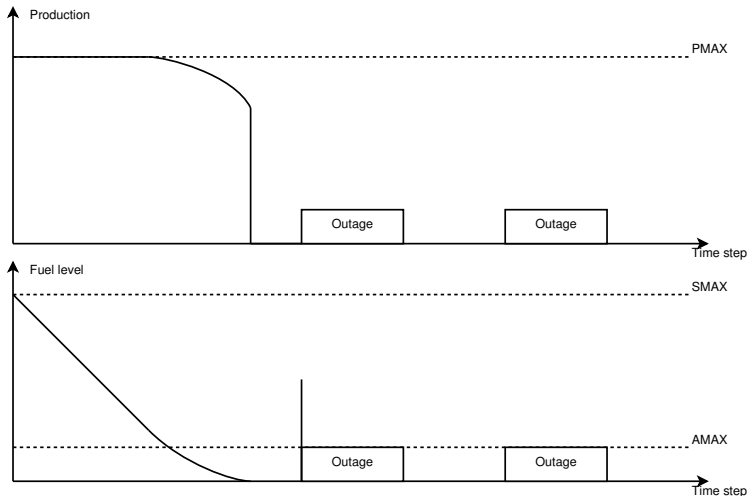




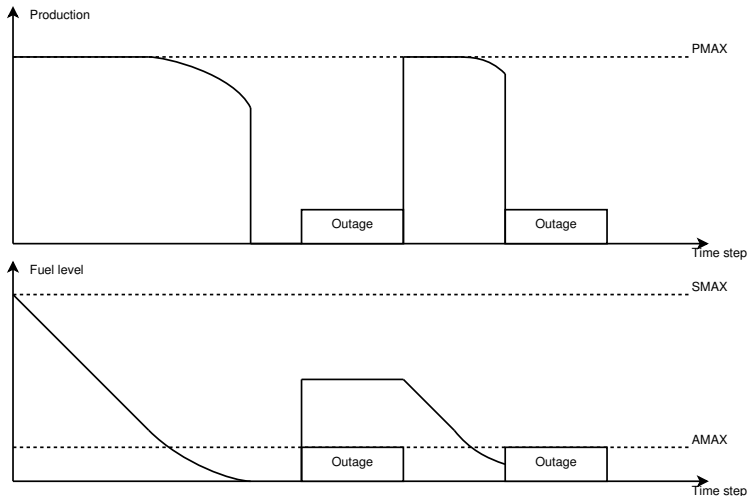
## Greedy production planning, cont'd



# Greedy production planning, cont'd



## Greedy production planning, cont'd

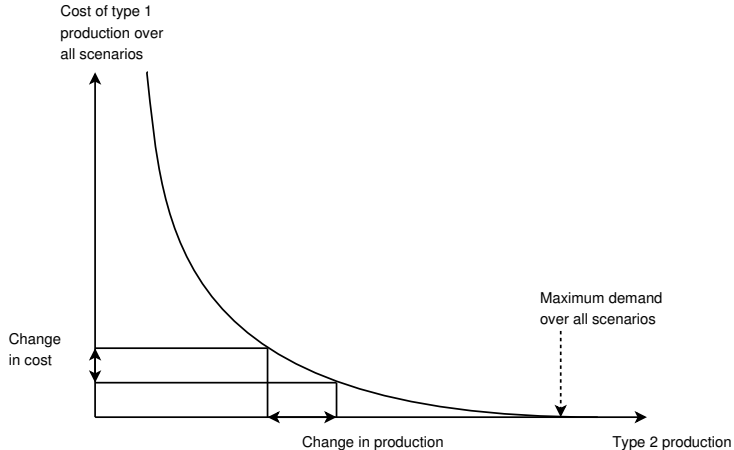


# Local search

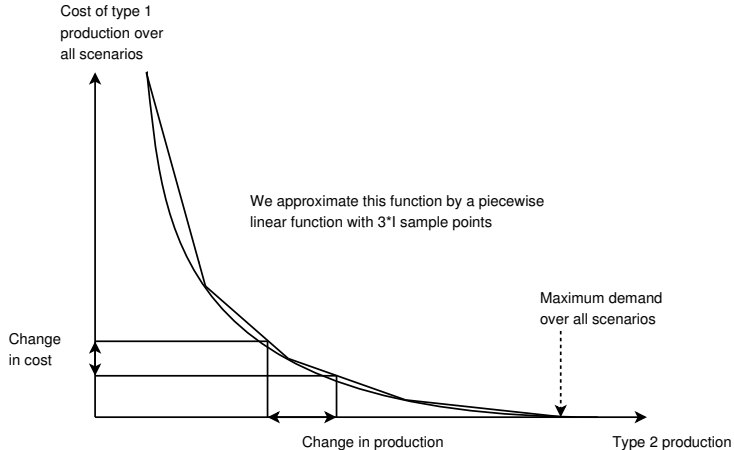
We try to improve on the outage schedule by local search

- Initial solution: We start from the CP-solution
- The neighborhood consist of all possibilities of moving a single outage a few weeks forwards or backwards
  - We only consider moves that are feasible wrt. CT13 to CT21
  - We only consider moving outages less than  $m$  weeks
- Evaluation: A move is evaluated by the estimated change in production cost. The change consists of changes in
  - Type 2 costs for the affected plant: Re plan production and refuel amounts
  - Type 1 costs: Estimation of the effect over all scenarios.

# Estimating the change in type 1 cost



# Estimating the change in type 1 cost



This approximation to type 1 costs is relatively good:

- In our experience it is correct up to 3 or 4 significant digits
- Evaluating the approximation is a constant time operation, since we maintain the total type 2 production for every time step

But somewhat memory expensive:

- Need to store an approximation for each time step

# Meta heuristic, simulated annealing

To guide the local search we use a simple simulated annealing procedure

- Start temperature that gives an acceptance ratio of approximately 0.5
- Exponential cooling with plateaus
- Restart after  $n$  idle iterations



# Modulation strategy

To make the solution feasible we modulate the type 2 power plants according to the minimum demand scenario.

- Idea: Modulate on the type 2 plant which has the shortest time to the next outage.

It is better to modulation per scenario, as we will see now.

# Results

Instance	Results (competition)	Results (per sc. mod.)
dataB6.txt	$8.5511 \cdot 10^{10}$	$8.5544 \cdot 10^{10}$
dataB7.txt	$8.1900 \cdot 10^{10}$	$8.1912 \cdot 10^{10}$
dataB8.txt	$8.3469 \cdot 10^{10}$	$8.2810 \cdot 10^{10}$
dataB9.txt	$8.3487 \cdot 10^{10}$	$8.2851 \cdot 10^{10}$
dataB10.txt	$8.0185 \cdot 10^{10}$	$7.9150 \cdot 10^{10}$

**Table:** Computational results

The per scenario results are for instances B8, B9 and B10 about 0.8%, 0.8% and 1.2% better respectively.

# Thank you for your attention!

# Questions?